ORIGINAL PAPER

Biological Cybernetics

Online learning and control of attraction basins for the development of sensorimotor control strategies

Antoine de Rengervé · Pierre Andry · Philippe Gaussier

Received: 27 August 2013 / Accepted: 27 November 2014 © Springer-Verlag Berlin Heidelberg 2014

Abstract Imitation and learning from humans require an adequate sensorimotor controller to learn and encode behaviors. We present the Dynamic Muscle Perception-3 Action(DM-PerAc) model to control a multiple degrees-offreedom (DOF) robot arm. In the original PerAc model, pathfollowing or place-reaching behaviors correspond to the sensorimotor attractors resulting from the dynamics of learned sensorimotor associations. The DM-PerAc model, inspired by human muscles, permits one to combine impedancelike control with the capability of learning sensorimotor 10 attraction basins. We detail a solution to learn incremen-11 12 tally online the DM-PerAc visuomotor controller. Postural attractors are learned by adapting the muscle activations in 13 the model depending on movement errors. Visuomotor cat-14 egories merging visual and proprioceptive signals are asso-15 ciated with these muscle activations. Thus, the visual and 16 proprioceptive signals activate the motor action generating 17 an attractor which satisfies both visual and proprioceptive 18 constraints. This visuomotor controller can serve as a basis 19 for imitative behaviors. In addition, the muscle activation pat-20 terns can define directions of movement instead of postural 21 attractors. Such patterns can be used in state-action couples 22 to generate trajectories like in the PerAc model. We discuss 23 a possible extension of the DM-PerAc controller by adapting 24 the Fukuyori's controller based on the Langevin's equation. 25 This controller can serve not only to reach attractors which 26

A. de Rengervé (⊠) · P. Andry · P. Gaussier ETIS UMR CNRS 8051, ENSEA, University Cergy Pontoise, 95000 Cergy Pontoise, France e-mail: rengerve@ensea.fr

P. Andry e-mail: andry@ensea.fr

P. Gaussier e-mail: gaussier@ensea.fr were not explicitly learned, but also to learn the state/action couples to define trajectories. 28

Keywords Visuomotor control · Impedance control · Perception–action loop · Neural network

1 Introduction

In order to act efficiently in unknown environments and 32 collaborate with humans, robots must be able to con-33 trol and adapt their behaviors. Contrary to the classical 34 motor control approach, human-robot interaction and imi-35 tation paradigms take into account that a human part-36 ner can influence and improve both the behavior and the 37 behavioral learning of a robot. Our past work, follow-38 ing a developmental approach (Lungarella et al. 2003), 39 along with collaborations with developmental psycholo-40 gists, cognitive psychologists, and neuro-biologists have 41 led us to understand that the tasks and behaviors cannot 42 be reduced to a set of controlled parameters. Behaviors 43 rather emerge from the dynamics of perception-action cou-44 pling (Gaussier and Zrehen 1995; Maillard et al. 2005). 45 The behavior is built upon a wide range of interactions at 46 different levels. A behavior learning system must be able 47 to capture the dynamical sensorimotor attractors describ-48 ing the behaviors. In such conditions, the issues of learn-49 ing, adapting, and sharing these attractors are fundamental 50 in order to achieve natural and intuitive nonverbal human-51 robot interaction. What are the constraints on the low-52 level motor control to learn such attractors? What kind of 53 model of motor control should be used and how can it be 54 learned? 55

Impedance control enhances optimal control in the case of interaction with the environment (Sect. 2.1). In impedance

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movements with respect to the desired trajectory. In the 59 framework of human robot interaction, regression-based 60 solutions (Ijspeert et al. 2003; Calinon et al. 2007) can learn 61 the desired trajectories from data obtained during the task 62 demonstration by a human (Sect. 2.2). The trajectories result 63 from mixtures of adapted kernels. Impedance control can be 64 linked to muscle activations (Sect. 2.3). Though, the hypoth-65 esis of a desired trajectory is usually kept while focusing 66 on the link between muscle activations and the impedance 67 control parameters (stiffness,...). On the contrary, we defend 68 the perception-action (PerAc) approach claiming that behav-69 70 iors correspond to sensorimotor attractors emerging from 71 the dynamics of multiple learned sensorimotor associations (Sect. 3). 72

control, position and velocity constraints determine the

In our first works on the emergence of imitation (Gaussier 73 et al. 1998; Andry et al. 2004), we showed that an arm 74 controller using the learning of visuomotor associations to 75 build a homeostatic controller can lead to the emergence of 76 low-level imitative behaviors if the perception is ambigu-77 ous (i.e. when mistaking partner's hand for its own hand). 78 However, this visuomotor controller had several limitations. 79 In particular, it did not allow the coding of trajectories by 80 state-action couples like in the PerAc approach. We thus pro-81 pose, in this paper, a model called Dynamic-Muscle PerAc 82 to control a robot arm with multiple degrees-of-freedom 83 (Sect. 4). The DM-PerAc model is based on simple models 84 of muscles and joints with dynamic equations correspond-85 ing to impedance control. This DM-PerAc model learns 86 the inverse kinematic model by learning visuomotor asso-87 ciations. It also learns postural attractors to link percep-88 tion (visuomotor categories) with actions coded as muscle 89 activations, i.e. it also learns the inverse dynamic model. 90 The behavior and properties of the DM-PerAc visuomo-91 tor controller are evaluated in Sect. 5. Like in our previous 92 works (Andry et al. 2004), the DM-PerAc visuomotor con-93 troller is a good bootstrap for imitative behaviors (Sect. 6.2). 94 In addition, the muscle activation patterns can be used in 95 state/action couples to code trajectories like in the PerAc 96 model (Sect. 6.1). In Sect. 6.3, we introduce Fukuyori's con-97 troller to improve performance and we discuss its possi-98 ble role to learn trajectories with the DM-PerAc model in 99 Sect. 7. 100

2 State of the art of online, incremental motor control for learning from interaction

103 2.1 Impedance control

In optimal control theory (Todorov 2007), the desired trajectory is an optimal trajectory crossing given via-points and

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minimizing some movement variables like jerk¹ (Flash and 106 Hogan 1985). The motor control should be flexible enough 107 to allow physical interaction with the environment. Studies 108 of movement properties have led to the impedance control 109 model (Hogan 1984) as an approximation of neuro-muscular 110 properties. According to the equilibrium trajectory hypothe-111 sis (Flash 1987), motor programs are internally represented 112 as the trajectories of an equilibrium point. Impedance con-113 trol is sufficient to control manipulators acting in contact 114 with the world (Chiaverini et al. 1999). Impedance control is 115 also a usual controller for prostheses and exoskeleton which 116 involve direct physical interaction with a human (Jiménez-117 Fabián and Verlinden 2011). Impedance control is based on a 118 second order "damped mass spring"-like system (1) enabling 119 constrained motion, dynamic interaction and obstacle avoid-120 ance. 121

$$M\frac{dV}{dt} = K(X_0 - X) + B(V_0 - V)$$
(1) 122

where V is the velocity and X is the Cartesian position of 123 the end effector. The coefficient K (equivalent to the spring 124 stiffness) and B represent the constraints related to the posi-125 tion command X_0 and the speed command V_0 , respectively. 126 Some other versions of impedance control use the proprio-127 ceptive information (e.g. Albu-Schäffer et al. 2007) instead of 128 the Cartesian position. In addition, the via-points, which are 129 necessary to compute the desired trajectory $(X_0(t), V_0(t))$, 130 can be learned from watching (Miyamoto and Kawato 1998). 131

2.2 Learning tasks from a human with regression techniques

The trajectories can be directly learned from training data 134 obtained during a task demonstration by a human. In order to 135 learn how to fulfill a task, a human teacher can provide feed-136 back or data which are integrated in a sensorimotor model 137 of the task. Function approximation based on local regres-138 sion techniques (Atkeson et al. 1997) is sufficient to learn 139 forward or inverse models of robot control. Learning an ini-140 tial model from a human demonstration reduces the size 141 of the space to be explored. Demonstrations facilitate and 142 improve subsequent reinforcement learning (Schaal 1997). 143 More recent, the Locally Weighted Projection Regression 144 algorithm (LWPR) (Vijayakumar et al. 2005) merges both 145 the incremental learning properties of the Receptive Field 146 Weighted Regression (RFWR) algorithm (Schaal and Atke-147 son 1998) and the projection of input data in order to reduce 148 the dimensionality problem. The authors showed a demon-149 stration with a 30DOF SARCOS humanoid robot learning 150

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¹ In the minimum-jerk approach, the movements maximize the smoothness of the motion.

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the dynamic inverse model and performing eight-shaped tra jectories with its arm.

Regression techniques to learn models of motor con-153 trol were also used in learning from demonstration para-154 digm (Argall et al. 2009). The Dynamic Movement Prim-155 itives (DMP) (Ijspeert et al. 2003, 2013; Schaal 2006; Hoff-156 mann et al. 2009) are based on the RFWR algorithm. The 157 primitives are control policies that are activated depending 158 on a local basis function. They provide motor control as a 159 second-order dynamic system. The combination of primitive 160 shapes in the attractor landscape produce the desired trajec-161 tory. This combination depends on a phase variable which 162 163 gives the temporal reference of the movement. The approximated function is the time-dependent trajectory, and locally 164 weighted regression of training data determine the parame-165 ters of the basis functions (number, centers, bandwidths) and 166 the contribution of corresponding primitives. The DMP algo-167 rithm shows interesting properties of spatial and temporal 168 invariance and was applied to learn discrete and rhythmic 169 movements. However, the correspondence problem (Nehaniv 170 and Dautenhahn 2002) was completely eluded as the train-171 ing data were obtained from a joint-angle recording system 172 on the human. A particular coupling must be introduced 173 in the dynamic equation of the phase variable in order to 174 tackle correctly perturbations. The action of this coupling is 175 to slow the evolution of the phase variable when there are 176 perturbations. 177

Similarly, a Gaussian Mixture Model (GMM) can also 178 learn a model of a demonstrated task by encoding proprio-170 ceptive and Cartesian information in Gaussian kernels (Cali-180 non et al. 2007). The learning is based on an Expectation-181 Maximization process which adapts the Gaussian kernels 182 to describe probabilistically the input data obtained in a 183 training session. Then, given partial information such as 184 only the Cartesian position, Gaussian Mixture Regression 185 extracts the probable proprioception to control a robotic 186 arm. Depending on the task, vision or motion capture 187 devices can track particular elements (e.g. spoon, human 188 head) (Calinon et al. 2010a,b). Still, the computation of 189 the 3D Cartesian coordinates of the visual markers requires 190 particular calibrations of the external devices. Calinon et 191 al. (2009) uses a dynamical second-order motor controller 192 and Hidden Markhov Models (HMM) instead of GMM. 193 HMM encodes the sequential dependencies in the task, 194 whereas the motor controller now implements impedance 195 control. A trade-off between the position constraint and 196 the speed constraint is managed depending on the vari-197 ance in the demonstrated trajectories. This version of the 198 model is similar to DMP. The main difference is that 199 the learning of the constraints on the position and the 200 velocity profile can take into account the mutual influ-201 ence between different degrees-of-freedom, which is not 202 the case with DMP. Some recent works (Kronander and 203

Billard 2012; Rozo et al. 2013) studied the online adap-
tation of the control stiffness from the position varia-
tions and haptic feedback. This adaptation of the control
improved the quality of the collaboration between human and
robot (Rozo et al. 2013).204205206

2.3 Adaptation of muscle activations and impedance control 209

In the case of human arm control, the actions are gener-210 ated by muscle contraction. The VITE model (Bullock and 211 Grossberg 1989) is based on equations describing the muscle 212 activations. The resulting dynamics is similar to the dynam-213 ics produced by an impedance controller (Hersch and Bil-214 lard 2006). However, the VITE model also assumes a target 215 position to drive muscle activations. In iterative and adap-216 tive control (Slotine 1988), the behavior can be adapted by 217 changing the control parameters instead of changing the com-218 mand. Considering the adaptation properties at the level of 219 muscular control (Burdet et al. 2006; Franklin et al. 2008), 220 the authors proposed a muscle-centered model of adaptive 221 and iterative control to maintain a posture or to follow a 222 trajectory under disturbances (Ganesh et al. 2010). The con-223 troller takes into account a feedforward torque command and 224 a feedback control to generate the final torque command. 225 The feedforward torque command is generated by muscular 226 activation. The feedback controller is a proportional deriv-227 ative. Such control can be equivalent to impedance control 228 if the apparent inertia is assumed to vary and to be equal 229 to the inherent inertia of the robot. The muscle activations 230 are adapted in order to reduce the feedback error. Indeed, 231 in the model (Ganesh et al. 2010), the adaptation of the 232 muscle activities directly induces changes of the feedfor-233 ward torque and of the stiffness in the feedback controller. 234 Feedforward torque modification enables one to compen-235 sate for an applied external force. In the case of rapidly 236 varying disturbances, the stiffness of the feedback con-237 troller is increased, so the robustness of the controller also 238 increases. However, increasing the stiffness from a muscu-239 lar point of view is energy consuming. Thus, the stiffness 240 will tend to decrease when the unpredictable perturbations 241 cease to occur. This model permits maintaining a desired 242 posture or following an a priori given trajectory. The princi-243 ple of adapting the muscle activations should not be reduced 244 to adapting the parameters of the impedance control. This 245 principle is also interesting to learn the perception-action 246 coupling. 247

3 The perception-action model and arm control

For many years, we have defended the perception–action 249 approach (PerAc, Gaussier and Zrehen 1995) claiming that, 250 in an active system, coupling perception and action enables 251



Fig. 1 a PerAc model. **b**–**d** Examples of built dynamics in 2D spaces. **b** Fixed point attractor. **c** Limit cycle in the case of a navigation experiment. **d** Trajectory following. In **b** and **d**, the *gray dotted lines* are the Voronoi boundaries. The *plain black line* is a trajectory sample

building of behaviors. Fast online learning of associations 252 between sensory signals and motor signals is sufficient to 253 build sensorimotor attraction basins. Let us consider the sen-254 sorimotor system of an agent acting in a given environment 255 (or state space) and having two sensation vectors \mathbf{X}_r and 256 \mathbf{X}_{ϱ} (Fig. 1a). Firstly, the proprioception vector \mathbf{X}_{r} repre-257 sents the coarse feedback information from the execution 258 of the motor command or the direction of the goal (if the 259 goal is in the immediate neighborhood). It can be considered 260 a reflex or a regulatory pathway that links proprioceptive 261 sensation to the motor command Ac. Secondly, the global 262 sensory vector \mathbf{X}_g represents more global information about 263 the environment. A local but robust distance measure (met-264 ric) can be computed to compare global sensory vectors. In 265 the PerAc model (Fig. 1a), the global sensory vector is cat-266 egorized and a competition (soft-WTA) between the cate-267 gories allows to define recognition activities R. On the basis 268 of the distance measure, the categories which best represent 269 the current state are determined. Categories are associated 270 with concurrent actions estimated from the proprioceptive 27 vector \mathbf{X}_r . An action field is thus defined. This action field 272 associates particular actions (movement vectors or forces) 273 to areas of the state space according to the recognized cate-274 gories. Depending on the built action field, the dynamics of 275 the system can be shaped to produce interesting behaviors, 276 e.g. attractor points, limit cycles, or trajectories. Figure 1b-277 d shows examples of dynamics defined in a 2D space. In 278 Fig. 1b, d, the Voronoi diagram shows for any point of the 279 space which category wins the recognition competition. The 280 associated action is thus performed as long as the state of 28 the system is in the same Voronoi area. A trajectory sam-282 ple is given in Fig. 1b. The system reaches the boundary 283 of the Voronoi area where it started, then it follows this 284

boundary to the defined attractor point. Whatever the ini-285 tial position is, the learned dynamics leads the system to the 286 attractor point with a similar kind of trajectory. The attrac-287 tion basin emerges from the system dynamics generated by 288 the state/action couples. Figure 1c shows a configuration of 289 action field that produces a limit cycle. No time basis is nec-290 essary. As the system moves, it reaches another area of the 291 action field and performs the corresponding action which 202 brings and maintains the system close to the followed limit 293 cycle. Not using a time basis has several advantages. No 294 synchronization of the time reference is needed, which is 295 quite a complex process, especially when there are pertur-206 bations of the trajectory. The learning is also more direct, 297 and can be performed online very rapidly because the model 298 simply learns what should be done in a directly sensed 299 context. 300

A similar kind of state/action combination can also pro-301 duce a simple trajectory following (Fig. 1d) Indeed, partial 302 limit cycle construction can provide a dynamics with which 303 the system behaves as if it is "attracted" by a trajectory and 304 remains in its close vicinity. In the state/action configuration 305 of Fig. 1d, the system can only get closer to an "equilibrium" 306 path where, due to the alternate category recognition, the 307 effects of the associated actions tend to equilibrate. The sys-308 tem is maintained in the vicinity of this path. Depending on 309 the orientation of the learned movement actions, the system 310 will tend more to reach the trajectory or to move forward. 311 By allowing the system to come back to the trajectory, the 312 PerAc model can manage perturbations. 313

The PerAc model has been proven to be an efficient con-314 trol for navigation and path following (Giovannangeli et al. 315 2006), with good robustness against perturbations such as 316 obstacle avoidance. In these works, the learned categories 317 are place-cells based on visual recognition of the robot's 318 location (see Giovannangeli et al. 2006 for details). The 319 state/action associations are learned online from interaction 320 with a teacher (Giovannangeli and Gaussier 2010). When 321 the robot moves away from the desired trajectory, the human 322 teacher changes its orientation to correct its behavior. This 323 feedback is used to learn new place-cell/orientation cou-324 ples to complete the sensorimotor control and to modify 325 the robot's behavior. This sensorimotor learning enables the 326 robot to follow trajectories (limit cycles, Fig. 1c) and even 327 to reach particular locations which become attractors for the 328 dynamical system. In the PerAc approach, the perception is 329 considered to be the result of learning sensation/action asso-330 ciations allowing a globally consistent behavior while fac-331 ing an object. For instance, by learning sensorimotor asso-332 ciations, a robot can learn how to return to a given object 333 which can be interpreted as the robot is "perceiving" the 334 object (Maillard et al. 2005). 335

The same sensorimotor association principle can be a basis ³³⁶ for the emergence of low-level imitative behaviors (Gaussier ³³⁷

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et al. 1998). In the case of arm control, we showed (Andry et 338 al. 2004) that an imitation of directly observed gestures can 339 appear as a side effect of a homeostatic visuomotor controller 340 with perceptual ambiguity. During a first phase, the system 341 learns associations between visual and motor signals build-342 ing a visuomotor homeostat. Because of low visual capabil-343 ities, the robot is unable to discriminate its own hand from 344 the hand of a teacher (ambiguity of perception). As the con-345 trol architecture implements a homeostat, the system tends 346 to maintain the equilibrium between visual and propriocep-347 tive information. If a difference is perceived, then the system 348 349 acts to come back to the equilibrium state. To do so, the robot moves its arm so that its proprioceptive configuration 350 corresponds to the perceived visual stimuli according to its 351 sensorimotor learning. As a result of these movements, the 352 demonstrator's gestures are imitated (Andry et al. 2004). The 353 correspondence problem (Nehaniv and Dautenhahn 2002) is 354 avoided as the robot only imitates what is observed with its 355 own capabilities. 356

In the model of Andry et al. (2004), Lagarde et al. (2010), 357 the control was performed in the visual space. A forward 358 kinematic model allowed the estimation of the visual position 359 of the robot hand. This position was then compared with the 360 perceived visual position to generate movements (see Andry 361 et al. 2004 for details). A first drawback was that erratic esti-362 mations of the visual position of the robot hand produced 363 an erratic control. Because the forward model learning was 364 based on Self-Organizing Maps (Kohonen 1982), false esti-365 mations could occur until learning convergence. Thus, the 366 controller should not be used before the end of learning. 367 The learning process was not incremental. Finally, the tra-368 jectories were not coded by sensorimotor couples like in the 369 PerAc model. Indeed, the motor commands were extracted 370 from the Dynamic Neural Fields (Schöner et al. 1995) by 371 using an ad hoc readout mechanism. This solution presented 372 interesting properties (memory, bifurcation) (see Sect. 5.4), 373 but was only able to define attractor positions. Moreover, 374 we were not able to explain how the readout process could 375 be learned or tuned. Here, we are interested in a model that 376 can bootstrap imitative behaviors and can also code trajec-377 tories according to the PerAc approach. The model should 378 also be incremental and able to manage multiple degrees-of-379 freedom. 380

In Iossifidis and Schoner (2006), Andry et al. (2004), the 381 authors developed arm controllers which work in spaces dif-382 ferent from the motor space, reducing the number of dimen-383 sions. The difficulty is then to extract a motor command from 384 the control in the lower dimension space. In the DM-PerAc 385 model, we use the alternate solution consisting of perform-386 ing the control in the proprioceptive space. The generation 387 of the motor command is simplified, whereas the difficulty 388 is to learn sensorimotor attractors. The resulting motor con-389 troller should be able to learn either a particular movement 390

or a postural attractor. In the next section, we describe the 391 Dynamic-Muscle PerAc (DM-PerAc) model which provides 392 a common coding basis for both aspects of the control. The 393 DM-PerAc model is based on a simplified model of joints 394 and muscles where both particular movements and postural 395 attractors are coded as muscular activations. We also detail 396 how the DM-PerAc model learns visuomotor attractors. 397

	4	Dyna	amic-n	iuscle	PerAc	model
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We now present our model, Dynamic-Muscle PerAc, to con-399 trol a robotic arm. This model combines control equivalent to 400 impedance control with the PerAc principle. The parameters 401 and equations of the DM-PerAc model are all summarized 402 in the Appendix. 403

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4.1 Control of joint position with a simplified muscle model 404

Different models such as Hill's model (Hill 1938) and Hux-405 ley's model (Huxley 1957) have been developed describing 406 different properties of the muscles. In the lumped-parameter 407 nonlinear antagonistic muscle model (Winters and Stark 408 1985, 1987), the movements of a joint are produced by a 409 couple of antagonist muscles. The muscles are simulated by 410 Hill's muscle model. This model is based on three compo-411 nents: a contractile element, a series elastic element, and a 412 parallel elastic element. In Klute et al. (2002), the two elastic 413 elements are neglected to focus on the dominant contractile 414 element. The contractile element can be approximated by a 415 force generator in parallel with a damping element (Cook and 416 Stark 1968). The force generator implements the force-length 417 relation in muscles with the force that can be modulated by 418 neural signals (Winters and Stark 1987). The damping ele-419 ment implements the force-velocity relation given by Hill 420 (1938). 421

Our model, called Dynamic-Muscle PerAc (DM-PerAc), 422 is also based on couples of antagonist muscles (hereafter 423 noted + and -) around the joints with each muscle approx-424 imated as a contractile element. However, unlike (Klute et 425 al. 2002; Winters and Stark 1987), we use a simplified lin-426 ear model of a contractile element which generates torque 427 instead of force. In the DM-PerAc model, the torque gener-428 ator is a spring with variable stiffness, whereas the damping 429 element is a simple viscous damper (Fig. 2). The varying 430 stiffness is given by the muscle activations A. The joint posi-431 tions are controlled with the Eqs. (2-8). As these equations 432 are the same for each joint, the joint index *j* is not displayed. 433 In addition, the time step (t) dependency is only indicated to 434 disambiguate terms when different time steps are involved in 435 the same equation. For each joint, the agonist and the antag-436 onist muscles generate the apparent torques τ^+ and τ^- (2). 437

 θ^+ A^+,σ^+ A^-,σ^-

Fig. 2 Simplified model of muscle control relying on a spring damped model of muscles. Damping properties are hypothesized to be mechanical properties of the arm still related to the muscle stiffness

$$\begin{cases} \tau^+ = -A^+ \cdot \theta^+ - \sigma^+ \cdot \dot{\theta}^+ \\ \tau^- = -A^- \cdot \theta^- - \sigma^- \cdot \dot{\theta}^- \end{cases}$$
(2)

where A^+ (resp. A^-) is the muscle activation and σ^+ (resp. σ^-) is the damping² of the agonist (resp. antagonist) muscle. The angular values θ^+ and θ^- are measured respectively from the full flexion position θ_{max} and from the full extension position θ_{min} (3).

$$\theta^{+} = \theta - \theta_{\max}, \ \theta^{-} = \theta - \theta_{\min} \text{ and } \theta \in [\theta_{\min}, \theta_{\max}]$$
 (3)

with θ the angular position of the joint.

⁴⁴⁷ The dynamical equation of the system links the rotational ⁴⁴⁸ acceleration $\ddot{\theta}$ and the moment of inertia *I* with the torques ⁴⁴⁹ generated by the agonist and antagonist muscles given by (2) ⁴⁵⁰ and the torque τ_e given by external forces.

$$I \cdot \ddot{\theta} = \tau^{+} + \tau^{-} + \tau_{e}$$

= $-A^{+} \cdot \theta^{+} - \sigma^{+} \cdot \dot{\theta^{+}} - A^{-} \cdot \theta^{-} - \sigma^{-} \cdot \dot{\theta^{-}} + \tau_{e}$
(4)

Equations (3) and (4) gives the Eq. (5) where $\sigma = \sigma^+ + \sigma^-$

$$I \cdot \ddot{\theta} = A^{+} \cdot (\theta_{\max} - \theta) - A^{-} \cdot (\theta - \theta_{\min}) - \sigma \cdot \dot{\theta} + \tau_{e}$$
(5)

In the absence of external torques/forces ($\tau_e = 0$), the system defines an attractor at the convergence point $\theta_{eq} = \frac{A^+ \cdot \theta_{\text{max}} + A^- \cdot \theta_{\text{min}}}{A^+ + A^-}$. To simplify this controller, the angular positions θ of the joint are normalized so that for each joint, they vary between 0 and 1.

459 $\theta_{\min} = 0 < \theta < \theta_{\max} = 1, \quad \theta^+ = 1 - \theta \text{ and } \theta^- = \theta$ (6)

In this particular case, our control Eq. (5) is equivalent to (7) 460 with $\theta_{eq} = \frac{A^+}{A^+ + A^-}$ with $K = A^+ + A^-$.

$$\ddot{\theta} = \frac{K}{I} \cdot (\theta_{eq} - \theta) - \frac{\sigma}{I} \cdot \dot{\theta}$$
(7) 462

The Eq. (7) corresponds to a classical mass-spring damping 463 system with a stiffness K and an equilibrium position θ_{eq} . 464 The equilibrium position is unchanged when both A^+ and A^- 465 are multiplied by the same factor. Such a factor only modifies 466 the equivalent stiffness K. An adaptation of the stiffness K467 and the damping σ controls the rise time, overshoot, and settling time. The controller was simulated using discrete 469 time with a time increment Δt . With I the moment of inertia 470 and τ the sum of the torques $\tau = \tau^+ + \tau^-$, the equations of 471 the dynamical system are: 472

$$\begin{cases} \theta_t = \theta_{t-\Delta t} + \dot{\theta}_t \cdot \Delta t \\ \dot{\theta}_t = \dot{\theta}_{t-\Delta t} + \ddot{\theta}_t \cdot \Delta t \\ \ddot{\theta}_t = \tau_t / I \end{cases}$$
(8) 473

The variables θ_t , $\dot{\theta}_t$, $\ddot{\theta}_t$ correspond, respectively, to θ , $\dot{\theta}$, $\ddot{\theta}$ in the Eqs. (2–7).

In our model (5), the generated torque depends on the 476 activation A of the muscles and on the lengths of the mus-477 cles (angles θ). This dependance on the muscle length makes 478 our model look like the "lambda" model of Feldman (1966, 479 1986). In the Theory of the Equilibrium Point (Feldman and 480 Levin 2009), also called the Theory of Threshold Control, the 481 motor control is based on threshold functions (λ) defining the 482 activation of the agonist and antagonist muscles. However, 483 in our model, the activation thresholds are not controlled. 484 The activation of the muscles is directly the controlled para-485 meter. Therefore, our model is closer to the "alpha" model 486 as described in Bizzi et al. (1992). In the alpha model, the 487 generated torque is directly controlled by the muscle activa-488 tions producing the equilibrium point trajectories and adapt-489 ing the stiffness. Following our simple model of muscle, in 490 our model, the generated torques depend on both the acti-491 vation of muscles (i.e. their stiffness) and on the muscle 102 lengths. Our model has also a major difference from the 493 alpha model as it associates muscle activations with learned 494 visuomotor configurations instead of relying on a tempo-495 ral sequence of muscle activations. In the next section, we explain how the muscle activations are learned and asso-497 ciated with the recruited visuomotor categories in order to 498 allow motor control. 499

4.2 Categorization of proprioceptive and visual space 500

The DM-PerAc model can use the previously described simplified muscle model with learned visuomotor associations to build a visuomotor controller (Fig. 3). Visual and pro-

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 $^{^2}$ The damping can be constant. However, controlled movements are improved if the damping varies with the stiffness. For instance, the damping can be defined as proportional to the square root of the stiffness like in Ganesh et al. (2010).



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Fig. 3 Architecture of the visuomotor arm controller. Both visual and proprioceptive information are categorized. The visual input is associated with the proprioceptive input. The visuomotor categories are then

prioceptive signals are merged into visuomotor categories 504 which are associated with the muscular activations deter-505 mining the arm movements, i.e. defining postural attractors. 506 First, we present how the visual and proprioceptive cate-507 gories are learned and computed. In the next section, we 508 will present how the visuomotor categories are built from 509 the learned visual and proprioceptive categories. We will 510 also detail how the postural attractors are learned as muscle 511 activations associated with the visuomotor categories. Both 512 processes occur alternatively and participate in the sensori-513 motor babbling process, allowing the robot to learn how to 514 act. 515

Proprioceptive categories are recruited during a senso-516 rimotor exploration process. Considering the agonist/anta-517 gonist muscles, the proprioceptive information is defined by 518 the angular positions of the controlled joints $\mathbf{P} = [\theta_1^+ \dots$ 519 θ_N^+ $\theta_1^- \dots \theta_N^-$] (index m).³ Each value $\theta^{+/-}$ is positive and 520 normalized with respect to the agonist or antagonist refer-521 ences (see Fig. 2). The categorization of the proprioceptive 522 input is described by (9) and (10). The proprioceptive inputs 523 **P** are encoded into categories \mathbf{S}^{P} with Gaussian responses 524 depending on a variance parameter β^{P} . The variance para-525 meter β^{P} enables increasing or to reducing the selectivity 526 of the sensory categories. They are recruited with a process 527 based on Adaptive Resonance Theory (Carpenter and Gross-528 berg 2002). If the current input **P** is too different from any 529 encoded sensory pattern \mathbf{W}_{i}^{P} , i.e. if the recognition \mathbf{S}_{i}^{P} is under a vigilance threshold λ^{P} , then a new category i_{r} is 530 531

associated with the muscle activations defining the motor attractors. The visual input activates the associated visuomotor categories and thus the corresponding motor attractors

recruited ($\varepsilon^P = 1$). The current sensory input **P** is stored on the weights $\mathbf{W}_{i_r}^P$ to the i_r th category. Even though a slow adaptation of the encoded categories is also possible, we do not consider it in this article.

$$\begin{cases} S_i^P = exp\left(-\frac{\sum_m (P_m - W_{im}^P)^2}{2\beta^P}\right) \\ \Delta W_{i_r j}^P = \varepsilon^P \cdot (P_m - W_{i_r m}^P) \\ \text{with } \varepsilon^P = \mathscr{H}(\lambda^P - \max_i(S_i^P)) \end{cases}$$
(9) 536

with the Heaviside function $\mathscr{H}(x) = 1$ if x > 0 and 0 537 otherwise. The recognition activities \mathbf{S}^{P} are normalized to 538 give the output of the recognition process \mathbf{R}^{P} (10). 539

$$R_i^P = \frac{S_i^P}{\sum S^P} \tag{10}$$

The output R_i^P can be interpreted as the probability that the sensory category *i* is the current sensory state of the robot. In practice, we approximated the sensory categorization process to a winner-takes-all which corresponds to the variance parameter β^P tending to 0, i.e. the selectivity for the categories R_i^P is maximal.

In our robotic setup, the visual information is captured by a single camera. A visual feature detector (e.g. color detector) enables extracting points of interest. The information is then projected over two 1D fields or vectors using population coding. Each vector codes the accumulated salience for the projected points of interest. The retina-centered vectors are then converted into body-centered vectors by a transformation

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³ Bold letters indicate vectors, whereas plain letters are scalars.

562

using the pan and tilt angles of the camera. The body-centered 554 vectors are computed as dynamic neural fields (Schöner et al. 555 1995). Thus, they exhibit bifurcation and memory properties 556 which are interesting in this attentional processing context. 557 The coordinates (v_1, v_2) of the maximally salient points in 558 this field are considered the visual input. The visual cate-559 gories are updated and learned using the Eq. (11) based on 560 the Eq. (9). 561

$$\begin{cases} R_k^V = \frac{S_k^V}{\sum S^V} \text{ with } S_k^V = exp\left(-\frac{\sum_l (V_l - W_{kl}^V)^2}{2\beta^V}\right) \\ \Delta W_{k_r l}^V = \varepsilon^V \cdot (V_l - W_{k_r l}^V) \\ \text{ with } \varepsilon^V = \mathscr{H}(\lambda^V - max_k(S_k^V)) \end{cases}$$
(11)

The recruitment of a visual category R_k^V increases the vigilance threshold λ^P of the proprioceptive categorization in order to facilitate the recruitment of a proprioceptive category if none already encodes the current posture.

4.3 Associating learned visuomotor categories with muscle activations

The visual and proprioceptive signals are merged in a visuo-569 motor layer. There is a bijection between the proprioceptive 570 categories and the visuomotor categories. Whenever a new 571 proprioceptive category is recruited, a new visuomotor cate-572 gory S_i^{VM} is also recruited and associated with it. The visuo-573 motor category is then associated with the muscle activations 574 A maintaining the categorized posture. The aim of the visuo-575 motor learning process is to determine which visual category 576 R_k^V is maximally activated when the arm reaches the attrac-577 tor posture S_i^P . The connection weights W_{ik}^{VM} are increased depending on the co-activated visual (R_k^V) and propriocep-578 579 tive (S_i^P) categories (12): 580

$$\Delta W_{ik}^{VM} = \varepsilon^{VM} \cdot S_i^P \cdot (f(S_i^P) \cdot f(R_k^V) - W_{ik}^{VM})$$
(12)

with ε^{VM} a constant learning rate. The function f is defined by $f(X_l) = 1$ if $X_l = max_l(X_l)$ and $f(X_l) = 0$ otherwise. The co-activation is only learned when the arm is close enough to the posture S_i^P , so the learning is modulated by the factor S_i^P that checks if the similarity measure S_i^P is high enough. Incorrect visuomotor associations can be progressively forgotten.

The activities of the neurons in the visuomotor layer are computed with the following Eq. (13):

$$\begin{cases} R_i^{VM} = \frac{S_i^{VM}}{\sum S^{VM}} & \text{with } S_i^{VM} = R_i^P \cdot \sum_k \left(g\left(W_{ik}^{VM}\right) \cdot R_k^V \right) \\ g(W_{ik}^{VM}) = 1 & \text{if } \left(\frac{W_{ik}^{VM}}{\max_k(W_{ik}^{VM})}\right)^n > 0.5 \\ 0 & \text{otherwise} \end{cases}$$

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A weight W_{ik}^{VM} contributes either as a factor 1 or 0 in 593 the update equation. The connection with maximal weight, 594 among the input connections to a neuron *i*, always gives a 595 factor equal to 1. Other connections can be "active" (factor 596 equal to 1) if their weights are close enough to the maximum. 597 Several visual categories can then activate the same visuomo-598 tor category. The normalization of the activities of the visual 599 categories R_k^V ensures that the activities of the visuomotor 600 categories $S^{\tilde{V}M}$ are always smaller than 1. The saturation of 601 the neural activities is thus avoided. In addition, when the 602 exponent *n* tends to $+\infty$ only the connection with maximal 603 weight is equal to 1 and any others are null. We consider this 604 particular case in the experiments. 605

The learning is performed online and fast. It is also incre-606 mental. By modifying some parameters (vigilance λ^P / λ^V or 607 variance β^P / β^V) of the sensory categorization process, new 608 visual and proprioceptive categories can be added online and 600 are directly available for the visuomotor control. The vigi-610 lance parameter determines how much categories can over-611 lap. Increasing the vigilance, i.e. allowing more overlapping, 612 will increase the number of recruited categories. The vari-613 ance parameter of the Gaussian kernels can be decreased 614 with a similar result. If the variance is reduced, the selectiv-615 ity of the categories increases and more categories will be 616 recruited. Maintaining the vigilance level enables maintain-617 ing a certain level of overlapping and thus of interference 618 during learning. 619

As a result of a visuomotor association learning, a visual 620 input can elicit visuomotor categories which activate motor 621 actions (muscle activations) to drive the arm to the propri-622 oceptive configuration associated with the visual constraint. 623 When a new visuomotor category is recruited, the muscle 624 activations which enable maintaining the visuomotor config-625 uration (in practice, maintaining the proprioceptive configu-626 ration is enough) are learned. Muscle activation coefficients 627 are learned online in a perception-action process. The sen-628 sorimotor loop is essential. As the system acts, it corrects or 629 modifies its motor commands online to maintain the desired 630 posture of the arm. The corrective movements are learned 631 by increasing the adequate connection weights to the muscle 632 activation neurons $\mathbf{A} = [A_1 \dots A_{2N}] = [\mathbf{A}^+, \mathbf{A}^-]$. The 633 activities of the visuomotor categories \mathbf{R}^{VM} determine the 634 muscle activations A with (14): 635

$$A_m = \sum_i W^A_{mi} \cdot R^{VM}_i \tag{14}$$

where the weight W_{mi}^A is the learned activation of m^{th} muscle to maintain the arm in the proprioceptive configuration *i*. In order to learn the muscle activations, the proprioceptive configuration corresponding to a recruited visuomotor category is stored. This proprioceptive signal \hat{P} is then used as a supervision for the muscle activation learning. The desired 640

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position \hat{P}_m is learned in one shot by associating **P** to $R_{i_r}^{VM}$ when the i_r th visuomotor category is recruited. The corresponding update and learning equations are (15):

$$\hat{P}_{max} = \sum_{i} W_{mi}^{\hat{P}} \cdot R_{i}^{VM} \text{ with } W_{mi_{r}}^{\hat{P}} = P_{m} - W_{mi_{r}}^{\hat{P}}$$
(15)

During the muscle activation learning process, the system 647 selects a visuomotor configuration that is to be learned (for 648 instance, the last recruited visuomotor category i_r). The robot 649 tries to reach the visuomotor configuration using the associ-650 ated proprioceptive configuration \hat{P} to correct movements. 651 This selection means that only the target visuomotor configu-652 ration is active (with i_r the selected configuration, $R_{i_r}^{VM} = 1$ 653 and $R_{i\neq i_r}^{VM} = 0$), so only the corresponding weights W^A are 654 modified. When the system learns the muscle activations, no 655 other visuomotor category can be learned, and the visuomo-656 tor exploration is suspended. The exploration resumes when 657 the motor control meets the condition (no more correction). 658 The learning Eq. (16) is based on a positive and a negative 659 term and one learning factor: 660

$$\Delta W_{mi}^{A} = \mathscr{H}(L - th_{L}) \cdot (\varepsilon^{A} \cdot C_{m} \cdot R_{i}^{VM} \cdot (1 - W_{mi}^{A}))$$

$$-\alpha^{A} \cdot W_{mi}^{A} \cdot \max_{i} [K_{j} - nc]^{+})$$
(16)

where ε^A is a learning rate, α^A is a decay rate and $[x]^+ = x$ if 663 x > 0 and 0 otherwise. The positive term in (16) increases the 664 muscle activations, thus changes the attractor so that the equi-665 librium posture matches the desired posture \hat{P} . This adapta-666 tion is based on the correction signal C detailed below (17). 667 The role of the negative term in (16) is to normalize the stiff-668 ness K_i of the joints j to the constant value $nc.^4$ As the 669 negative term changes all muscle activations with the same 670 factor α^A , it does not modify the equilibrium posture, only 671 the stiffness is modified. This normalization process is nec-672 essary to avoid the saturation of both the weights W_{mi}^A and 673 the neural activities A_m which would prevent any further 674 correction of the movements. 675

The part of the architecture in the gray rectangle in Fig. 4 is dedicated to the computation of the correction signal *C*. For each joint, the signal *C* compares the desired movements \mathbf{M}^{D} with the current movements \mathbf{M} (17) to determine if a muscle should contract more, i.e. if the muscle activations associated with the target visuomotor configuration should be increased.

$$C_m = \mathscr{H}(M_m^D - M_m) \tag{17}$$

Each neuron in the desired movement layer M^D evaluates the need to contract the muscle m ($M_m^D = 1$ or 0) to correct the posture. To do so, the equation of M_m^D (18) determines if



Fig. 4 Neural network learning the muscle activations to maintain the robotic arm in desired proprioceptive configurations. Learning is based on a neuromodulation process increasing the weights W_{mi}^A so the muscle activations **A** enable maintaining the desired posture. A second neuromodulation loop induces the normalization of the stiffness **K** of the different joints to avoid saturating the muscle activations

the muscle "length" P_m (i.e. θ^+ or θ^-) should be reduced to match the desired "length" \hat{P}_m .

$$M_m^D = \mathscr{H}(P_m - \hat{P}_m - th_D) \tag{18}$$

where th_D is a threshold under which no correction is 690 requested. It defines the accuracy constraint for the move-691 ments. The correction signal C_m (17) does not change the 692 muscle activations if the current movement M_m already 693 reduces the muscle length, i.e. if P_m is decreasing. This 694 condition allows avoiding overshooting the correction of 695 the movements. This condition is computed by $M_m(t) =$ 696 $\mathscr{H}(P_m(t - \Delta t) - P_m(t))$ with $M_m = 1$ when no change of 697 the muscle activation should occur. 698

The learning factor $(\mathscr{H}(L - th_L))$ induces learning of muscle activations during a variable period of time depending on the comparison between the "learning enabling" signal *L* and the threshold th_L . This signal *L* evaluates the need to continue adapting the muscle activations (19).

$$L(t) = \left[\mathscr{H}(L(t - \Delta t) - th_L) \cdot \sum_m [C_m - \hat{C}_m]^+ + \gamma^L \cdot L(t - \Delta t) + t_g(t)]^+$$
(19) 704

In our implementation, the learning is triggered $(t_g(t) = 1;$ 0 otherwise) when a new visuomotor category i_r is recruited. Therefore, the muscle activations are directly learned after the recruitment of each visuomotor category, ensuring that motor commands are associated with all visuomotor categories. Yet, the muscle activation learning may also be triggered by other signals, such as a random signal arbitrarily 711

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⁴ In practice, the range of activities was [0, 1] and we used nc = 0.1.

724



Fig. 5 Webots simulation of a Katana arm. Learning a postural attractor in the 4DOF motor space. The evolution of the muscle activation and of the resulting equilibrium point is given for the 2nd articulation of the arm. A uniform random noise ([-0.5, 0.5]) is added to the torque command. When the movement of a joint is in the direction opposite to

the target direction, the corresponding muscle activation is increased. As the stiffness increases, the shift of the position of the equilibrium point at each correction becomes smaller to enable performing a gradient descent toward the target position. In addition, a bigger stiffness increases the robustness to the noise

selecting categories to refine the associated motor command. 712 The muscle activation learning continues as long as there 713 is an unexpected correction of the muscle activations. Such 714 unexpected correction is determined by comparing for each 715 muscle occurring correction C_m with its prediction \hat{C}_m . The 716 occurrence of an unexpected correction increases the value of 717 the signal L, thus extending the learning time period. The for-718 getting factor γ^L modulates the time period during which no 719 unexpected corrections must occur before the attractor adap-720 tation ends. The prediction $\hat{\mathbf{C}}$ of the corrections is learned 721 by conditioning with C the unconditional stimulus and \mathbf{R}^{VM} 722 the conditional stimulus (20). 723

$$\hat{C}_m = \sum_i W_{mi}^C \cdot R_i^{VM} \quad \text{with } \Delta W_{mi_r}^C = \varepsilon^C \cdot R_{i_r}^{VM} \cdot (C_m - \hat{C}_m)$$
(20)

The learning rate ε^{C} is small to have a memory effect. The 725 learned muscle activations are expected to maintain the arm 726 close to the postural target, so no more corrections are neces-727 sary. The learning of this posture can then stop and the motor 728 exploration resumes. Sometimes the arm may be blocked by 729 an obstacle (possibly itself). The current version of the archi-730 tecture does not include an obstacle avoidance process (still, 731 a security module can block movements to prevent damages), 732 so the muscles may only be more and more contracted with-733 out correcting the position. The deadlock is broken when the 734 prediction $\hat{\mathbf{C}}$ of the continuous correction finally compen-735 sates the detected correction C and stops the learning. The 736 motor exploration can then resume and the muscle activa-737 tions related to this unsuccessfully learned postural attrac-738 tor are not used for the control. Interestingly, in Redgrave 739 and Gurney (2006), the authors hypothesized that the role 740 of dopamine could also be to detect novelty and maintain 741 or repeat recent actions providing the adequate context for 742 learning. In our case, detecting unpredicted situations (cor-743

rections) can maintain the learning of a given posture instead of resuming the motor exploration. 744

As mentioned above, the weights W_{mi}^A and the muscle activations **A** are bounded ($\mathbf{A} \in [0, 1]^N$) due to the learning rule (16). Hence, the muscle activations **A** are multiplied by a constant stiffness factor *G* increasing the amplitude of the apparent stiffness. The resulting equilibrium point is unchanged, whereas the apparent stiffness is now equal to $G \cdot K$. The previous dynamic Eq. (5) becomes (21): 750

$$I_{j} \cdot \ddot{\theta}_{j} = G \cdot (A_{j}^{+} \cdot (\theta_{j,max} - \theta_{j}) - A_{j}^{-} \cdot (\theta_{j} - \theta_{j,min}))$$

$$-\sigma_{j} \cdot \dot{\theta}_{j} + \tau_{j,e} + \eta_{j}$$
(21) 754

For each joint j, a noise term η_j is also added in the motor 755 command producing varying exploratory movements to help 756 the learning of the muscle activations. 757

5 Experimental results

5.1 Postural attractor learning

The process to learn postural attractors was tested and vali-760 dated in a simulation⁵ of the Katana arm used in our robot-761 ics experiments (Figs. 5, 6). In this experiment, the external 762 torque τ_e was null. As the arm moves, the muscle activa-763 tions are increased so that each joint is maintained at the 764 desired position (Fig. 5). The progressive adaptation of the 765 muscle activations depends on random movements (7). Still, 766 the arm finally stabilizes at the desired posture (Fig. 6). 767 As the muscle activations increase, the shifts of the equi-768 librium point due to learning become smaller and smaller. 769 This property results from the ratio in the equation of the 770 equilibrium point $\left(\theta_{j,eq} = \frac{A_j^+}{A_j^+ + A_i^-}\right)$. Thus, the equilibrium 771

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⁵ With the software Webots (Cyberbotics).

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Fig. 6 The attractor learning test is reproduced 10 times. *Left*: Mean position of the learned attractor for joint 2 with the limits of the *gray area* representing the standard deviation. *Right*: Average and standard deviation of Euclidean target distance in the normalized joint space. The *red line* is the distance constraint th_D for each joint proprioception. The mean distance to the target decreases down to this constraint

position converges to the desired position while the stiff-772 ness $(K_j = A_i^+ + A_i^-)$ increases. The behavior adapta-773 tion is quite slow because of the low frequency of the hard-774 ware control loop of the Katana arm (about 7 Hz). Another 775 major constraint is the speed encoding in the robot arm 776 firmware. Very low speed is not available because of the 777 discretization of the values. Instead of an unnatural freez-778 ing of movements when the speed should be very close 779 to null, the articulations keep rotating at the fixed mini-780 mal speed. In fact, these small oscillations give a more nat-781 ural aspect to the idle movements of the arm. The feeling 782 of a frozen system is avoided during human-robot interac-783 tion. In this experiment, there was no external torque. The 784 reason is that the servo controllers of the Katana electrical 785 robotic arm are not compatible with external perturbations. 786 This is a strong limitation of the hardware. We performed 787 simulations to show that our model can also manage this 788 case. 789

5.2 Maintaining a particular posture under external torque 790

In order to show that our model can also cope with external 791 torques, we use a simple simulation of a 1D arm (Fig. 7a). 792 First, the muscle activations are learned in the case of a 793 gravitational torque (Fig. 7b-c). In the equation of con-794 trol (21) the external torque is the following gravitational 795 torque $\tau_e = -ma * g * le * sin(\theta)$ with mass ma, gravity 796 constant g = 9.81, and length *le* between the rotational axis 797 and the gravity center. In order to compensate for this torque, 798 the muscle opposing gravity contributes more to maintain 799 the posture (Fig. 7c). This solution is more energy efficient 800 and accurate than simply increasing the overall impedance. 801 It corresponds to the change of reciprocal activation level 802 observable in human motor behaviors in equivalent circum-803 stances (Franklin et al. 2008). The movements resulting from 804 the learn controller are shown in Fig. 7d. Figure 7e shows that 805 the error made is indeed below the accuracy threshold used 806 during learning. 807

We also tested the impact of increasing the noise level of 808 η_i (in (21)) which corresponds to stochastic perturbations 809 of the movements. If the controller was learned with a low 810 noise level, the movements are strongly perturbed by the 811 noise. The position error while maintaining the learned pos-812 ture has a strong variance (Fig. 7f). Then the postural attractor 813 was learned with the increased noise level (Fig. 7g-h). As a 814 result, the muscle activations are also increased, which cor-815 responds to increasing the stiffness (Fig. 7h). Thus, the pro-816 duced movements are less perturbed by the noise (Fig. 7i-j). 817 Our model can learn how to maintain posture control under 818 a gravitational torque, and it can also increase the stiffness 819 of the movement to resist to stochastic perturbations during 820 learning. 821



Fig. 7 a A simple 1D model of an arm is used to test muscle activation learning under gravitational torque. The parameters are g = 9.81, ma = 2 kg and le = 0.4 m. The angle θ is normalized with respect to the movement range $[0, 5\pi/4]$. **b** Trajectories for 30 samples of posture control learning. **c** Evolution of the muscle activations during learning. The muscle opposing gravity contributes much more than the other one.

d 10 examples of trajectories produced by one of the learned posture controllers. **e** Corresponding position error with respect to the target (0.85). **f** The noise level η_j is increased (from 0.1 to 1.5). The movements are then less accurate. **g–h** The posture control is learned as in **b-c**, but with the increased noise level $\eta_j = 1.5$. **i–j** As a result, the accuracy in reaching the target position is improved (lower variance)



Fig. 8 Simulation of online learning and adaptation of sensorimotor attractors with a 4DOF arm and a 2D camera. Left-hand column presents the results after an initial sparse learning and the *right-hand* column gives the results after learning continued with learning parameters inducing more selectivity in the state recruitment. a During the motor babbling, the robot recruits visual states (red diamonds) and proprioceptive states (black circles). Each proprioceptive state is associated with one visual state (blue link). b After learning, the visual input is artificially switched to a star-shaped trajectory in the visual space (dark *line*). According to the visual state recognition, the robot moves so the arm end effector trajectory tries to follow the visual input (gray dashed line). c Movements performed in the 3D Cartesian space during the star shaped trajectory reproduction. d As the parameters changes, the robot can complete its previous learning by recruiting more visual states and proprioceptive states. e The movements of the arm matches more closely to the star shaped trajectory in the visual space. f Corresponding movements in the 3D Cartesian space

822 5.3 DM-PerAc visuomotor controller

We validated the visuomotor controller in the same 3D sim-823 ulation of a Katana robot arm as in the previous section. In 824 Fig. 8a-c, the robot performs a motor babbling with parame-825 ters inducing a low selectivity, and thus a very low level of 826 accuracy for the recruited visual and proprioceptive states. A 827 simple test to evaluate the visuomotor learning is to reproduce 828 a trajectory given in the visual space. A star-shaped trajectory 829 is given as visual input to the system (Fig. 8b). The trajectory 830 resulting from the visual processing of the arm end effector 831 tracking is displayed. The robot tries to follow the trajectory, 832 but because of its sparse learning, the performance is very 833 limited. In the developmental process of the robot, the para-834

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Fig. 9 Comparison between the trajectories from initial (*Left-hand column*) and consecutive learning (*Right-hand column*). Initial learning: mean error 6.0 degrees, standard deviation 3.5 degrees. Consecutive learning: mean error 4.3 degrees, standard deviation 2.5 degrees

meters determining the sparsity of learning may be changed 835 to recruit more visual and proprioceptive categories (Fig. 8d-836 f). The new visuomotor attractors are integrated online to the 837 initial learning. The performance of the system is increased. 838 Figure 9 displays the visual trajectories of the desired and 839 real position of the arm end effector. The mean square error 840 is shown with the mean error and the standard deviation to 841 compare the evolution of the performance with the inclu-842 sion of more attractors. The same kind of performance could 843 have been obtained by directly learning with the parameters 844 increasing the selectivity of the coding. 845

To sum up Figs. 8 and 9, learning a postural attractor 846 takes time, and learning many attractors will slow the explo-847 ration of the whole motor space, but provide a better coding 848 resolution, and therefore, a more accurate trajectory. Thus, 849 very accurate trajectories could only be reproduced at the 850 cost of a longer exploration and learning phase. In previ-851 ous studies (Andry et al. 2004) we have simulated with the 852 PerAc model that the learning time of all the possible senso-853 rimotor associations of a 6DOF model of the Katana robotic 854 arm with a high resolution CCD camera would require hun-855 dreds of thousands of movements. Taking a mean approxi-856 mation of the time necessary to perform one simple move-857 ment with our mechanical robot, we have calculated that 858 the whole exploration and learning of all the possible cat-859 egories would require more than 3 years (without optimiza-860 tion). This amount of time is still applicable to the DM-PerAc 861 model, since the number of possible categories (if we con-862 sider purely the maximal amount possible) is similar. Of 863 course, such a computation is a caricature, since the creation 864 of categories is by definition a means to avoid systematic 865 learning. 866

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Nevertheless, several considerations lead us to think that 867 such algorithms are consistent with the developmental course 868 of a human baby : 869

- This time course (several years) taken as an order of 870 magnitude is acceptable, compared to the time needed 871 to develop the coordination of the whole human body 872 (even if we limit to the coordination of one arm or one 873 hand). We just have to refer to the time needed to master 874 some movements in sports such as a golf swing, or the 875 time to learn to write. Progressive learning is still present 876 after months or years. 877

- If the maximal learning time is very long, DM-PerAC allows a very fast learning of simple trajectories with 10 to 20 attractors. The robot can thus perform simple tasks even if with limited accuracy. This fast acquisition of coarse and elementary actions is crucial in terms of behavior, and is consistent with developmental psychology: coarse actions support early imitation to communicate before the age of 9 months (Butterworth 1999), or object grasping before the age of 9 months (Law et al. 2014), and of course early sensorimotor exploration before the first year (Gergely 2001).

In addition to these elementary actions, the DM-PerAc 889 model can let the category creation continue in order to 890 improve the capabilities of the robot. New visual and pro-891 prioceptive categories can be recruited while the motor 892 babbling is resumed. Therefore, the robot can continu-893 ously evaluate the co-occurring proprioceptive and visual inputs to improve its visuomotor model with the newly 895 learned categories. The visuomotor associations can be 896 progressively updated as the system continues its bab-897 bling. 898

Altogether, these characteristics allow speculation about 899 when the babbling should stop. We can formulate the 900 hypothesis that the visuomotor babbling goes on while 90 the agent has not received remarkable repeated feedback. 902 The feedback could be purely "physical" (for example, 903 a tactile sensorimotor contingency when an object is 904 grasped) or "social" (the expression of a caregiver) and 905 modulate the strength of the learning. Thus, fast coarse 906 actions and long progressive learning can be complemen-907 tary in a global progress loop. 908

Interestingly, classical developmental psychology studies 909 also observe that such progress loop are guided by the 910 cephalocaudal (the more the limbs are far from the head, the 911 later they are available and mature to be implied in actions) 912 and the proximodistal (the more the articulation are far from 913 the root of the limb, the later they are available and mature 914 to be implied in actions) laws. These laws reflect constraint 915 of the body development that imposes a step by step process 916 of the motor control. One of the consequence of this scheme 917

is to constrain a coarse to fine learning where each change 918 in the child's development result in an increasingly refined 919 level of skill development (Santrock 2005).

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In Droniou et al. (2012), several regression algorithms 921 (including LWPR Vijayakumar et al. 2005) were compared 922 on the visuomotor control learning and performance. The 923 evaluation task is target tracking by the arm end effector of 924 a robot. The system must produce the movements to reach 025 a target given by its visual position, thus the learned inverse 926 kinematic models are compared. A stereo camera detects the 927 target, and its 3D Cartesian position is computed. In most of 928 the tests, the target follows a star-shaped trajectory path in 020 a vertical plane. The regression algorithms learn a forward 930 kinematic model in order to perform the tracking, thus focus-931 ing the exploration process on the motor space to perform 932 the task. The forward model allows estimating the Jacobian 933 matrix of the kinematic model, the inversion of this matrix, 934 and the 3D position of the target that provide the motor con-935 trol of the robotic arm. In this article, we have tested the DM-936 PerAc visuomotor controller on tracking a target moving on a 937 star-shaped trajectory. In our experiment protocol, the visuo-938 motor learning is open-ended. Also, the target coordinates 939 are simulated (no occlusion) in the 2D visual space. The 940 trajectories after learning are comparable to those obtained 941 in Droniou et al. (2012). Still, the regression techniques pro-942 duce smoother trajectories more accurate at the points of the 943 star path. However, inverting the Jacobian matrix requires 944 a specific processing in order to avoid singularities. Such a 945 matrix inversion is not satisfying from the perspective of the 946 developmental approach and is also difficult to model as a 947 biologically plausible process. 948

5.4 Bifurcation property of the DM-PerAc controller

We compare the properties of the DM-PerAc controller with 950 the properties of the Dynamic Neural Field based controller. 951 Dynamic Neural Fields (DNF) based on the Amari equa-952 tion (Amari 1977) are a solution to motor control used to 953 navigate (Schöner et al. 1995; Giovannangeli et al. 2006) or 954 to control a robotic arm (Iossifidis and Schoner 2004; Andry 955 et al. 2004). Biological studies showed that the activations 956 of some neurons in the motor cortex are correlated with the 957 direction of the movement to be performed (Georgopoulos 958 et al. 1986). In DNF, the activity profile of the field takes the 959 shape of a Gaussian centered on the input stimuli. Besides, 960 the derivative of the activity profile can provide the dynamics 961 of the control (Schöner et al. 1995). Dynamic Neural Fields 962 have interesting dynamical properties: memory to filter non-963 stable or noisy stimuli, and bifurcation capabilities enabling 964 reliable and coherent decisions when multiple stimuli are 965 presented. 966

In Fig. 10, we show that (i) the trajectories generated by the 967 DM-PerAc model can be analyzed and integrated to build the 968

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Fig. 10 Bifurcation capabilities in the DM-PerAc controller. *Top row* **a**-**b** shows the trajectories (*blue lines*) and the two learned attractors (*black dashed lines*). The *middle row* **c**-**d** displays the angular velocity profiles in function of the proprioception θ . The *bottom row* **e**-**d** gives the perception activity profile equivalent to the activities in a Dynamic Neural Field. In the *left-hand column*, the learned attractors are distinct whereas in the *right-hand column* they are closer, resulting in one merged behavioral attractor

DNF equivalent profile of activity, and (ii) there are bifurca-969 tion capabilities in our controller. In our tests, the state space 970 is [0, 1]. Trajectories generated by the DM-PerAc controller 971 are averaged into the actions $Ac(\theta)$ depending on the state of 972 the system (position). In practice, $Ac(\theta)$ is discretized into 973 a vector with components that are the values for different θ . 974 The result is thus the velocity profile given in Fig. 10c and d. 975 In Maillard et al. (2005), we proposed that the action Ac is 976 the derivative of a potential function defining the perception 977 of the system. The action Ac is thus spatially integrated to 978 obtain the perception Per (22). 979

980
$$\forall k, Per_k = \int_{[0,k/n]} Ac(\theta) d\theta + cste$$
 (22)

where *Per* is a vector of dimension *n* with components equal to the integration of the action *Ac* at different positions $\theta = k/n$. The integration constant *cst* is chosen so the maximal component value of *Per* is equal to 1. The perception profile *Per* is equivalent to the activity profile of a DNF, and shows bifurcation properties (see Fig. 10). The DM-PerAc model can produce behaviors similar to those obtained with the use

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Fig. 11 a Trajectories in 1D space with an asymmetric muscle activation pattern (a muscle is inactive). Trajectories start from different random positions. Activation signals are $G \cdot A^+ = G \cdot K = 5$, $A^- = 0$. The control parameters are $\sigma = 5$, $\Delta t = 0.05$ and the moment of inertia I = 1, **b**-c Attraction basins in a bounded 2D space $[0, 1]^2$ with DM-PerAc model. Given the learned position/movement couples (black diamonds, thick black lines), a force-field is generated (small gray points and lines). For each joint, only one of the agonist/antagonist muscles is activated as in a). Initial (circle) and final (square) points of the trajectories are indicated. b Vector field corresponding to one learned proprioception/activation couple. c, d Four state/action couples are learned. Four trajectories with different starting points are represented in the 2D state space. With only four couples, the system can learn a loop trajectory. The size of the loop depends on the speed, thus is related to the damping σ and the stiffness K. $\mathbf{c} \sigma = 10, G \cdot K = 10$. $\mathbf{d} \sigma = 5, G \cdot K = 10$. The other parameters of the system are the time increment $\Delta t = 0.05$ and the moment of inertia I = 1

of an explicit DNF without the need to define the whole field.988However, the property of memory is not directly available in
the model, but some other processes could complete the DM-
PerAc architecture to obtain this property.988

6 Use and extensions of the DM-PerAc model 992

6.1 Encoding trajectories with the DM-PerAc controller

It is possible to use the learned postural attractors in a time-994 based sequence with the attractors that are successively and 995 transiently activated. This process was used in the work 996 described in Sect. 6.2. However, the DM-PerAc architecture 997 is not limited to using this kind of trajectory coding. Now, 998 we consider the case where only one of the muscles around a 999 joint is activated (activation different of 0) while the other one 1000 is inactive. This configuration of activation signals induces 1001 movement toward the extreme limit of joint (full flexion or 1002 extension) (Fig. 11a). At the lower level of motor control, 1003 the muscle activations can be either interpreted as defining a 1004 postural attractor or as defining locally the movement to be 1005 performed (orientation and strength). As explained in Sect. 3, 1006

such associations between sensory categories and actions can 1007 define trajectories. The studied task is simply to reproduce 1008 a loop in the 2D motor space. Among four encoded states, 1009 each of them are associated with two 1D controllers, i.e. four 1010 muscle activation coefficients each. The muscle activations 1011 correspond to the demonstrated direction of movement. For 1012 each joint, only one of the muscle activations (agonist or 1013 antagonist) is different from null. An example of a vector 1014 field in 2D space defined by one state/action couple is given 1015 in Fig. 11b. An attraction basin can effectively be generated 1016 (Fig. 11c, d). The trajectories in the 2D state space show that 1017 the stiffness K and the damping σ control the movement 1018 1019 speed, and thus can change the size of the loop. Trajectories could be encoded using the low-level state/muscle activation 1020 associations. This coding can thus be a basis for both posture 1021 1022 and trajectory encoding. In the next section, we will focus on learning stable postural attractors. 1023

6.2 Imitative behaviors with the DM-PerAc controller

The visuomotor controller based on the DM-PerAc model 1025 can be used for the emergence of low-level imitative behav-1026 iors and can even be a basis for deferred imitation. An arm 1027 controller, based on learning visuomotor associations, can 1028 let low-level imitation emerge (Andry et al. 2004). In a first 1029 phase of babbling, the robot learns its body schema as mul-1030 tiple associations between the visual position of its arm end 1031 effector and the joint configuration of its arm. If the robot's 1032 visual perception is limited enough (using only movement 1033 information or the detection of colored patches), the robot 1034 can look at the hand of an interacting human and still believe 1035 it is its own hand. According to the previously learned visuo-1036 motor associations, this situation can induce an incoherence 1037 between the visual information from the teacher's hand and 1038 the motor information from the hand of the robot. As the 1039 controller is a homeostat, it tends to maintain equilibrium 1040 between the visual and the motor signals. Thus, the robot 1041 tries to reduce the visuomotor incoherence by moving its 1042 hand to match the visual input. Low-level imitation emerges 1043 as the movements of the robot follow the movements of the 1044 human (Fig. 12). In the next stage of development of the 1045 robot, this low-level visuomotor controller can be the basis 1046 for learning from observation. We consider that the learning 1047 robot can now memorize the sequence of the visual posi-1048 tions demonstrated by the teacher while it is inhibiting its 1049 own movement (de Rengervé et al. 2010). Then, as the robot 1050 internally rehearses the encoded visual sequence, the pre-1051 dicted visual position of the next state can be given to the 1052 low-level visuomotor controller. The robot reproduces the 1053 demonstrated sequence of gestures according to what was 1054 perceived during the demonstration. The robot is capable 1055 of doing some deferred imitation (de Rengervé et al. 2010, 1056 2013). 1057



Fig. 12 Example of imitation behaviors. *Left*: Low-level imitation of meaningless gestures. Qualitative comparison of imitated gestures performed in front of the robot. Perception ambiguity and a homeostatic controller induce movements to maintain perceptual equilibrium. The robot performs low-level imitation of directly observed gestures. *Middle and right*: Gesture imitation can be used to bring the arm end effector toward objects (here, to grasp a can) or interesting parts of the environment. It can become a common basis for learning by observation and learning by doing

6.3 Attractor selection and visuomotor control refining

The refining potential of the DM-PerAc model can be enhanced by the Yuragi (fluctuations)-based attractor selection model (Fukuyori et al. 2008) which relies on the following Langevin's Eq. (23): 1062

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$$\Lambda \cdot \dot{\mathbf{x}} = \xi \cdot f(\mathbf{x}) + \eta \tag{23}$$
 1063

where Λ is a time constant, the vector **x** describes the state of 1064 the system, and the function f is the dynamics of the attrac-1065 tor selection model. The main constraint that this attractor 1066 function f must respect is to define attractors. For instance, 1067 the function f can simply derive from a potential function 1068 with attractor points. Other particular examples of definitions 1069 of the function f can be found in Fukuyori et al. (2008), de 1070 Rengervé et al. (2010). When the coefficient ξ is big, the 1071 term $\xi \cdot f(\mathbf{x})$ predominates. The state of the system con-1072 verges to one of the attractors defined by f. Feedback on the 1073 current movement performance modulates the coefficient ξ . 1074 The feedback gives more influence to the attractor function 1075 f or to the stochastic exploration term η . As a result, the sys-1076 tem can switch from exploration between the different known 1077 attractors to exploitation of the closest attractors. According 1078 to the feedback, the function f can be adapted so that some 1079 attractors are shifted toward the desired positions. Thus, the 1080 desired positions can be learned. 1081

The principle of muscle activation learning (Sect. 4.3) 1082 in DM-PerAc is quite similar. The first difference is that 1083 the function f depends on the muscle contraction. During 1084 muscle activation learning, only one visuomotor category is 1085 active so only one postural attractor is active. The exploration 1086 is partly due to the noise on the motor command and also to 1087 the oscillations of the arm (when the stiffness is still low). 1088 During learning, the muscle activations are changed so that 1089 the resulting attractor is effectively shifted toward the desired 1090 position. Thus, this process can be seen as a low-level use of 1091 the Yuragi principle. 1092



Trajectory in visual space

(reaching learned position)

60 80 100 120

horizontal coordinate >

140 160

40

Fig. 13 Visual target reaching with a visuomotor controller using the "Yuragi" principle. The feedback is based on the target distance in the visual space. A known attractor can match the target (a, b) or the target can be between learned attractors (c, d). a, c Trajectories of the robot arm end effector in the visual space. The black circles correspond to the learned attractors and the black cross is the visual target to be reached. The stars are the starting positions for each trial, **b**, **d** Evolution of the distance between the arm end effector and the target in the visual space

(number of pixels). Dark gray dashed line shows the average distance

90

10

and target

 (\mathbf{h})

Graph of distance

(reaching a learned attractor

1000 1500 2000 2500 3000

iteration

The Yuragi principle can also be used in DM-PerAc when 1093 all the visuomotor categories are available. The movement 1094 dynamics is influenced by all the attractors associated with 1095 these categories and activated by visual and proprioceptive 1096 information. In that case, the Yuragi principle allows for 1097 improving the accuracy of the movements. In Fig. 13, we 1098 tested the reaching of a visual position using the Yuragi prin-1099 ciple (de Rengervé et al. 2010). The robot arm end effector 1100 reaches the visual target both when it is near the visual posi-1101 tion of a learned attractor (Fig. 13a, b) and when it is between 1102 the learned attractors (Fig. 13c, d). While performing tasks, 1103 the robot can use the Yuragi principle to reach targets which 1104 were not explicitly learned as attractors. When necessary, a 1105 new attractor could be recruited to learn how to reach a target 1106 that would otherwise be far to reach. The performance of the 1107 visuomotor controller could be improved for particular cases 1108 without recruiting many useless attractors. 1109

7 Conclusion-discussion 1110

Our previous works enabled the explanation of trajectory 1111 learning (PerAc model Gaussier and Zrehen 1995) and imi-1112 tative behaviors (Andry et al. 2004). Even though these differ-1113 ent works have in common the sensorimotor learning prin-1114 ciple, their properties could not directly be combined due 1115 to motor control issues. We propose the Dynamic Muscle 1116 PerAc (DM-PerAc) model to control a robot arm with mul-1117 tiple DOF (Sect. 4). It combines the principles of the PerAc 1118 model with a simple model of agonist/antagonist muscles 1119 where the muscle activations determine the movements of 1120 the robotic arm. The low-level motor control is equivalent 1121 to impedance control. The DM-PerAc model can incremen-1122 tally learn online the visuomotor control of the robot arm. 1123



to the attractors. The light gray line shows the threshold under which the target is reached. a Trajectories while reaching a learned attractor, two attractors activated, two trials with different starting positions. b Corresponding evolution of the target distance. c Trajectories while reaching a not previously learned position, four attractors activated, six trials with different starting positions. d Corresponding evolution of the target distance. In both cases, the arm end effector reaches the target, although, when it is not a learned position, the reaching can be quite long due to random exploration

During a motor babbling process, proprioceptive and visual 1124 categories are recruited and associated together (kinematic 1125 model) depending on co-activation. The DM-PerAc model 1126 then learns the postural attractors associated with the visuo-1127 motor categories to define the visuomotor control. Trajecto-1128 ries can also be coded by combining state/action couples such 1129 as in the PerAc model (Sect. 6.1). The states are associated 1130 with asymmetric muscle activations to generate movements 1131 in particular directions. In Sect. 6.2, we showed that imitative 1132 behaviors can be obtained with the DM-PerAc visuomotor 1133 controller. This controller can also be a basis for higher level 1134 encoding and imitation behaviors. 1135

Until now, we mainly tested the DM-PerAc model on a 1136 Katana robotic arm. However, the hardware of this robotic 1137 device is limited for impedance control. In particular, the 1138 servo controller of the Katana arm does not allow manag-1139 ing external perturbations such as gravitational torque. In 1140 Sect. 5.2, we showed in a simple 1D arm simulation that the 1141 DM-PerAc model can accurately learn a postural attractor 1142 under a gravitational torque. However, the impedance con-1143 trol was learned instead of performing an online adaptation 1144 to perturbations. In future work, the adaptation process will 1145 be added to the model. Also in future work, we will exploit 1146 the full potential of the DM-PerAc model to control move-1147 ments of a hydraulic torso robot called TINO.⁶ This robot 1148 was developed with the aim of allowing physical interaction 1149 and compliance. Impedance control is fully compatible with 1150 this hardware. With the DM-PerAc model, the visuomotor 1151 controller of the robot TINO can be learned. In addition, 1152

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⁶ The robot TINO was co-funded by the French projects INTERACT and SESAME TINO, the Robotex and the CNRS. The robot only recently arrived in the ETIS lab.

the DM-PerAc model is also a good basis to study imitative behaviors and interaction.

In this article, the motor control is based on a spring-based 1155 model of muscles; however, we do not pretend that modifying 1156 the stiffness of these spring-like muscles corresponds to an 1157 accurate model of neuro-muscular control. The rest-length of 1158 the muscles, motor reflexes, and other physiological proper-1159 ties are also important. Still, the aim of the DM-PerAc model 1160 is to allow sensorimotor dynamics learning with the gener-1161 ated behaviors that can be either attractor postures or trajec-1162 tory following. Using muscle activations has the advantage 1163 to make learning easier whatever the dynamics is (postural 1164 1165 attractor or trajectory).

The computational cost of the DM-PerAc visuomotor con-1166 troller can be reduced in different ways. The neurons corre-1167 sponding to categories (visual, proprioceptive, visuomotor) 1168 not yet recruited can be ignored in the neural update process. 1169 Also, the number of visual to visuomotor links (W^{VM}) may 1170 be reduced by using some lists of links dynamically managed 1171 according to the recognition of the visual and proprioceptive 1172 categories. This solution would allow the use of far fewer 1173 links than if considering the whole set of visual to visuomo-1174 1175 tor links.

We gave solutions to learn attractor points as they are 1176 used in the visuomotor controller for imitation behaviors. 1177 The learning of trajectories or paths is not described in this 1178 article. In the DM-PerAc model, postural attractors can be 1179 used as via-points to encode trajectories and we used this kind 1180 of solution in deferred imitation (de Rengervé et al. 2010). 1181 However, a correct encoding of dynamic trajectories should 1182 rely on state/action couples defining attraction basins, such as 1183 in the PerAc model (Sect. 3). The advantage is that agonist 1184 and antagonist muscles would not need to be active at the 1185 same time. The stiffness and the energy consumption can be 1186 reduced. In future work, we will study the activation patterns 1187 generated by this trajectory encoding model. In particular, 1188 we want to explore whether and how the state-action coding 1189 may allow the tri-phasic pattern of movement observed in 1190 humans (Sanes and Jennings 1984). 1191

Although we proved that the DM-PerAc model enables 1192 dynamical trajectory encoding, the learning of the adequate 1193 state/action couples is still an ongoing issue. In the PerAc 1194 model, the states and actions were associated by direct con-1195 ditioning. The orientation to follow (action) could be esti-1196 mated by integrating the followed orientation while moving. 1197 The orientation to follow could also be demonstrated to a pas-1198 sive robot. In the DM-PerAc model (Fig. 14a), a direct con-1199 ditioning is possible, but a particular process is necessary to 1200 extract the unconditional stimulus from a passive demonstra-1201 tion. Changes of proprioception cannot be directly converted 1202 into muscle activations (for instance, the muscle activations 1203 must change to perform the same movement manipulating 1204 objects with different masses). The Yuragi idea (Sect. 6.3), 1205



Fig. 14 a Possible solutions to learn muscle activations in the Dynamic Muscle PerAc model. **b** Example of dynamic trajectory with postural attractors and trajectory shaping constraints. Both components can be coded similarly in the DM-PerAc architecture

adapted to the DM-PerAc model, can be a potential solution to this issue. We believe that the Yuragi idea could allow locally learning combinations of attractors defining not only postural attractors, but also particular speed vectors. Still, the remaining issues are what the adequate feedback is and how it can be learned from a demonstration.

Finally, using the same encoding and the same kind of 1212 learning, the robot should be able to learn trajectories such as 1213 in Fig.14b mixing posture attractors and trajectory shaping. 1214

Acknowledgments This work was supported by the INTERACT 1215 French project reference number ANR-09-CORD-014. 1216

Appendix: summary of the parameters and equations 1217 used in the Dynamic Muscle PerAc model 1218

The different parameters and equations presented in this article are respectively summarized in Tables 1 and 2.

The proprioceptive (visual) categorization depends on the 1221 vigilance parameter λ^P (λ^V) and the parameter β^P (β^V) 1222 of the Gaussian similarity measure. High vigilance val-1223 ues would imply that recruited categories overlap. We use 1224 $\lambda^P = \lambda^V = 0.005$ to avoid interferences between categories. 1225 The values of the Gaussian parameters are very low so the 1226 categories are selective enough. During the learning step, dif-1227 ferent values are used to increase progressively the number 1228 of learned categories ($\beta^P = 0.002$ then $\beta^P = 0.001$, and 1229 $\beta^V = 2 \cdot 10^{-4}$ then $\beta^V = 5 \cdot 10^{-5}$). During the tests, vision 1230 must drive the movements, thus the proprioceptive categories 1231
 Table 1
 DM-PerAc Model: parameter summary with values used in experiments for the open parameters

- $\mathbf{A} = [A_1, \ldots, A_{2N}]$ muscle activation (stiffness)
- A^+ , A^- : activation of agonist (⁺) and antagonist (⁺) muscles for each joint ($A = [A^+, A^-]$)
- C: comparison of desired and current movements, determines the need to correct muscle activations, modulates the increase of W^A_{mi}
- $\hat{\mathbf{C}}$: prediction of \mathbf{C} for a given visuomotor category *i* in \mathbf{R}^{VM}
- G : stiffness factor, counterbalancing the bounded muscle activations A (ex: G = 60)
- K : stiffness
- i, i_m, i_r : indexes of proprioceptive category, winning proprioceptive category, and next recruited proprioceptive category
- **I** : moment of inertia (ex: I = 1)
- j: index of joint
- k, k_m, k_r : indexes of visual category, winning visual category, and next recruited visual category
- *l* : visual coordinates
- L : attractor learning signal

m: index of muscle

- \mathbf{M}^{D} , \mathbf{M} : desired muscle shortening, current muscle shortening
- n : exponent, used in the update of the visuomotor categories (ex: n = 100)
- N : number of joints
- \mathbf{R}^{P} , \mathbf{R}^{V} , \mathbf{R}^{VM} : normalized activities of \mathbf{S}^{P} , \mathbf{S}^{V} and \mathbf{S}^{VM}
- $\mathbf{P} = [P_1 \dots P_{2N}] = [\mathbf{P}^+ \mathbf{P}^-]$ proprioceptive input $\mathbf{P}^+, \mathbf{P}^-$: agonist and antagonist proprioceptive input
- $[\theta_1^+\theta_2^+\dots], [\theta_1^-\theta_2^-\dots]$
- $\mathbf{S}^{P}, \mathbf{S}^{V}$: recognition activities of proprioceptive and visual categories respectively
- \mathbf{S}^{VM} : visuomotor category, merging visual and proprioceptive signals
- $t, t \Delta t$: current time step, previous time step
- th_D : threshold on target distance to estimate desired movement (ex: $th_D = 0.01$)
- th_L : threshold on L under which current attractor learning is stopped (ex: $th_L = 10^{-5}$)
- V : visual input (coordinates in visual field)
- $\mathbf{W}_{im}^{P}, \mathbf{W}_{kl}^{V}$: learning weights to proprioceptive (\mathbf{S}^{P}) or visual (\mathbf{S}^{V}) categories
- \mathbf{W}_{mi}^{C} : learning weights to $\hat{\mathbf{C}}$
- \mathbf{W}_{mi}^{A} : learning weights to A
- \mathbf{W}_{ik}^{VM} : learning weights to \mathbf{R}^{VM}
- α^{A} : decay factor of muscle activation learning (\mathbf{W}_{mi}^{A}) (ex: $\alpha^{A} = 10^{-4}$)
- β^{P}, β^{V} : variance parameter of the Gaussian kernels of proprioceptive *P* or visual *V* categories.
- ε^{A} : learning factor of muscle activation (A) learning (ex: $\epsilon^{A} = 10^{-3}$)
- ε^{C} : learning factor of the predictor of **C** (ex: $\varepsilon^{C} = 0.2$)

Table 1 continued

- $\epsilon^{P}, \epsilon^{V}$: learning factor of proprioceptive P or visual V categorizations.
- γ^L : forgetting factor of the attractor learning signal *L* (ex: $\gamma^L = 0.95$)
- λ^{P}, λ^{V} : vigilance of proprioceptive categorization *P* or visual categorization *V*. (ex: $\lambda^{P} = \lambda^{V} = 0.05$)
- σ_j : damping (ex: $\sigma_j = 11$)
- $\theta_j, \dot{\theta_j}, \ddot{\theta_j}$: rotation angle of a joint, velocity, acceleration
- θ_j^+, θ_j^- : positive angular value measured in the agonist or antagonist reference (see Fig. 2)

 $\theta_{j,max}, \theta_{j,min}$: maximal and minimal angular value of a joint

- $\theta_{j,eq}$: equilibrium point resulting from muscle activations
- τ_j, τ_e : rotational torque, external torque

General tools

Heaviside function: $\mathscr{H}(x) = 1$ if x > 0, 0 otherwise Kronecker symbol: $\delta_{ij} = 1$ if i = j, 0 otherwise $[x]^+ = x$ if x > 0, 0 otherwise

Table 2 DM-PerAc Model: equation summary

Motor control based on commands of stiffness of agonist/antagonist muscles around the joints j^a

$$\tau_j = A_j^+ \cdot \theta_j^+ - \sigma_j^+ \cdot \dot{\theta}_j^+ - (A_j^- \cdot \theta_j^- - \sigma_j^- \cdot \dot{\theta}_j^-)$$

Which is simplified from additional constraints (6) as:
 $\ddot{\theta}_j = \frac{K_j}{L_i} \cdot (\theta_{j,eq} - \theta_j) - \frac{\sigma_j}{L_i} \cdot \dot{\theta}_j$ with $K_j =$

$$A_j^+ + A_j^-$$
 and $\theta_{j,eq} = \frac{A_j^+}{A_j^+ + A_j^-}$

- Update and learning of the proprioceptive and visual categories
- Proprioceptive categories (index *i*) based on the muscle proprioception $\mathbf{P} = [\theta_1^+, \theta_2^+, \dots, \theta_1^-, \theta_2^-, \dots]$ (index *m*):

$$S_i^P = exp\left(-\frac{\sum_m (P_m - W_m^P)^2}{2\beta^P}\right)$$

$$\Delta W_{i_rm}^P = \varepsilon^P \cdot (P_m - W_{i_rm}^P) \text{ with } \varepsilon^P = \mathscr{H}(\lambda^P - max_i(S_i^P))$$

Visual categories (index k):

$$R_{k}^{V} = \frac{S_{k}^{V}}{\sum S^{V}} \text{ with } S_{k}^{V} = exp\left(-\frac{\sum_{l}(V_{l} - W_{kl}^{V})^{2}}{2\beta^{V}}\right)$$
$$\Delta W_{k_{r}l}^{V} = \varepsilon^{V} \cdot (V_{l} - W_{k_{r}l}^{V}) \text{ with } \varepsilon^{V} = \mathcal{H}(\lambda^{V} - max_{k}(S_{k}^{V}))$$

Visuomotor association learning

 $\Delta W_{ik}^{VM} = \varepsilon^{VM} \cdot S_i^P \cdot (f(S_i^P) \cdot f(R_k^V) - W_{ik}^{VM})$ with $f(X_l) = 1$ if $X_l = max_l(X_l)$ and 0 otherwise

Visuomotor categories update

$$\begin{cases} R_i^{VM} = \frac{S_i^{NM}}{\sum S^{VM}} \text{ with } S_i^{VM} = R_i^P \cdot \sum_k (g(W_{ik}^{VM}) \cdot R_k^V) \\ \text{and } g(W_{ik}^{VM}) = 1 \text{ if } \left(\frac{W_{ik}^{VM}}{max_k(W_{ik}^{VM})}\right)^n > 0.5 \text{ and } 0 \text{ otherwise} \end{cases}$$

Postural attractor learning

Supervision signal based on incorrect movements:

$$\begin{cases} C_m = \mathscr{H}(M_m^D - M_m) \text{ where} \\ M_m^D = \mathscr{H}(P_m - \hat{P}_m - th_D) \text{ and} \\ M_m(t) = \mathscr{H}(P_m(t - \Delta t) - P_m(t)) \\ \hat{P}_m = \sum_i W_{mi}^{\hat{P}} \cdot R_i^{VM} \text{ with} \\ W_{mi_r}^{\hat{P}} = \varepsilon^P \cdot (P_m - W_{mi_r}) \text{ (on recruitment of a new } R_{i_r}^{VM}) \end{cases}$$

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